What Are Sources of Real Exchange Rate Fluctuations?∗

Keun Yeong Lee**

The paper investigates what sources of real exchange rate fluctuations are in a structural vector autoregression model for Korea vis-à-vis the United States. It first estimates three-variable VAR models with long-run zero restrictions and contemporary sign restrictions which are derived from the same theoretical model. The empirical results show that an important role of nominal shock in explaining real exchange rate fluctuations is not found in the both models. In addition, it estimates four-variable VAR models in which a nominal shock is separated by monetary policy and real exchange rate shocks. A monetary policy shock also does not have a strong influence on real exchange rate fluctuations. But a supply shock has a significant impact on them both in three- and four-variable VAR models.

JEL Classification: C3, E42, F31, F33
Keywords: real exchange rates, structural VAR, long-run zero restrictions, sign restrictions

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1. INTRODUCTION

Since the Korean exchange rate system had been transformed from the multi-currency basket system to the market average exchange rate system in March 1990, won/dollar exchange rates became to fluctuate highly through the periods of Asian currency crisis and global financial crisis. As already well known, it is difficult to linearly and nonlinearly forecast exchange rate changes between developed countries which are unconditionally leptokurtic and conditionally heteroskedastic. Won/dollar exchange rates also showed a similar pattern. In particular, after the market average exchange rate system was converted into the free floating exchange rate system in December 1997, this phenomenon became more severe to date. It was caused by the fact that won/dollar exchange rates were closely related to foreign macroeconomic variables as well as domestic macroeconomic variables in the aftermath of drastic openness of foreign exchange and financial markets. That is, real exchange rates under the open economy absorb spillover effects of domestic macroeconomic shocks and play an important role on mechanism of domestic spillover of foreign shocks. Hence, a lot of literature is recently eager to analyze the relationship between real exchange rates and fundamental macroeconomic variables. In case of Korea, because it is a small open economy with high dependence of foreign trade, spillover effects of foreign macroeconomic shocks have more severe impact on its economy.

As a representative example, Clarida and Gali (1994) analyzed impulse responses and variance decomposition of structural VAR with three variables such as output, prices, and exchange rates under the long-run zero restrictions. They found that nominal shocks did not play an important role in explaining exchange rate fluctuations. It implies that the exchange rate between main developed countries works just like a shock absorber. On the other hand, Farrant and Peersman (2006) estimated three- and four-variable VAR models with sign restrictions and discovered that nominal shocks played an important role in determination of real exchange rates in contrast to the empirical results of Clarida and Gali (1994). They showed that the exchange rate was
considered as a source of shocks, not a shock absorber. In case of won/dollar exchange rates, however, this kind of research based on long-run zero restrictions and sign restrictions is not carried out until now in spite of importance of relationships between output, prices, and exchange rates.

This paper estimates structural VAR models for Korea vis-à-vis the United States based on the two country open economy macroeconomic theory. It investigates interlinkage between real won/dollar exchange rates and fundamental macroeconomic variables such as relative industrial production, price level, and interest rates. The study first estimates structural VAR models with long-run zero restrictions and sign restrictions built on economic theories. Especially, using both estimation methods of Clarida and Gali (1994) and Farrant and Peersman (2006) which led to different conclusions, it examines whether or not real and nominal shocks play important roles in explaining won/dollar exchange rate changes. The paper also extends basic three-variable VAR models to four-variable VAR models by adding relative interest rates between both countries. It reconfirms whether it leads to the same conclusion or not. Finally, rolling regression analyses are performed in order to ascertain the possibility that the main results may be time-varying. In case of Korea vis-à-vis the United States, the sample period was not so long that it may lead to small sample biases. In addition, the exceptional periods such as the Asian currency crisis and the global financial crisis periods can distort estimation results. The long-run zero restriction assumptions also have the point in dispute in theoretical and empirical aspects. So these kinds of comprehensive analyses are required to solve these problems.

According to the empirical results, a nominal shock does not play a decisive role in elucidating won/dollar real exchange rate changes, when it uses three-variable VAR models which are composed of relative supply, demand, and nominal shocks under the long-run zero or sign restrictions. In case of four-variable VAR models in which a nominal shock is separated by monetary policy and real exchange rate shocks, a monetary policy shock does not have a strong influence on real exchange rate fluctuations, while a supply shock has a significant impact on them.
The subsequent sections of the paper are organized as follows. Section 2 reviews the studies which examine dynamic interrelationships between GDP, prices, and exchange rates using structural VAR models. Section 3 and 4 explain the estimation methods of VAR models based on long-run zero restrictions and sign restrictions. Section 5 derives impulse response functions and variance decomposition of forecasting errors from the estimation results. In section 6, their policy implications are examined. Section 7 summarizes and concludes the paper.

2. LITERATURE REVIEWS


Clarida and Gali (1994) developed the theoretical models of Dornbusch (1976) and Obstfeld (1985) into a VAR model of open economy with three relative variables and analyzed impacts of supply, demand, and nominal shocks on real exchange rates. They used a long-run triangular identification scheme proposed by Blanchard and Quah (1989) and found that demand shocks explained most of real exchange rate fluctuations. It means that the real exchange rate play a role as a shock absorber. The same conclusion was reached by Funke (2000) who investigated UK-Euro area and Chadha and Prasad (1997) who applied Clarida and Gali (1994) model to yen/dollar exchange rates. On the other hand, Artis and Ehrmann (2006) assumed the short-run zero restriction condition under which nominal shocks did not have contemporaneous impacts on output and showed that the exchange rate was not a shock absorber, but a source of shocks. Eichenbaum and Evans (1995) examined the effects of U.S. monetary policy on exchange rates with a VAR
model which assumed Cholesky decomposition.

In recent years, a lot of research estimated VAR models with sign restrictions on the basis of economic theories in various fields such as business cycles, exchange rates, and monetary and fiscal policies. For example, Faust and Roger (2003) relaxed identification assumption of existing research and then analyzed an effect of monetary policy on exchange rates. Scholl and Uhlig (2006) investigated a relationship between exchange rates and forward discount puzzle using sign restrictions. Farrant and Peersman (2006) examined Clarida and Gali (1994) model using sign restrictions instead of long-run zero restrictions and found that nominal shocks had permanent effects. The long-run zero restriction assumption is widely known to have problems of small sample bias, measurement error, and theoretical counterargument. In short, in contrast with the argument of Clarida and Gali (1994), they found that the exchange rate was not a shock absorber, but a source of shocks.

However, even though interactions between won/dollar exchange rates and key macroeconomic variables are very important from the standpoint of a small open economy, domestic analyses on their relationships under long-run zero restriction and sign restriction assumptions are not almost carried out to date. According to the empirical results in developed countries, impacts of nominal shocks on exchange rates are different, depending on whether long-run zero restrictions or sign restrictions are assumed. On the other hand, as Korea is a small open economy with complete openness of goods and financial markets, it is expected that won/dollar exchange rates are not significantly influenced by nominal and monetary policy shocks without regard to the assumption considered. The study focuses on whether this expectation is consistent with the empirical results or not.
3. ESTIMATION MODEL

The paper considers the following structural three-variable VAR model based on Clarida and Gali (1994).

\[ AZ_t = c + A Z_{t-1} + \cdots + A_p Z_{t-p} + u_t, \quad E(u_t'u_t') \equiv H, \]  
\[ AZ_t = c + A Z_{t-1} + \cdots + A_p Z_{t-p} + H^{1/2} \nu_t, \quad E(\nu_t'\nu_t') \equiv I. \]

Where \( Z_t = [\Delta y_t, \Delta q_t, \Delta p_t] \) is a \( 3 \times 1 \) endogenous variable vector and \( \Delta \) implies a first difference. Here \( y_t \) represents log industrial production relative to the US. \( q_t \) indicates the log real exchange rate of Korea against the US. The real exchange rate is defined such that an increase stands for a depreciation. \( p_t \) denotes log consumer prices relative to the US. Covariance matrices \( H \) and \( I \) are \( 3 \times 3 \) diagonal and identity matrices, respectively. \( u_t = [u_{i,t}, u_{d,t}, u_{n,t}]' \) or \( \nu_t = [\nu_{s,t}, \nu_{d,t}, \nu_{n,t}]' \) ( \( u_t = H^{1/2} \nu_t \) ) is the \( 3 \times 1 \) residual vector which are composed of three shocks such as supply, demand, and nominal shocks, and is not correlated with other variables and its own lagged variables. Equation (1) can be expressed as the following reduced-form.

\[ Z_t = A_1^{-1} c + A_1^{-1} A_1 Z_{t-1} + \cdots + A_1^{-1} A_p Z_{t-p} + A_1^{-1} u_t, \]  
\[ = d + B_1 Z_{t-1} + \cdots + B_p Z_{t-p} + \varepsilon_t, \quad E\varepsilon_t\varepsilon_t' = \Omega. \]

Using \( u_t = H^{1/2} \nu_t \), equation (4) can be expressed as follows.

\[ Z_t = X_t' \Theta + \varepsilon_t = X_t' \Theta + A_1^{-1} u_t = X_t' \Theta + A_1^{-1} H^{1/2} \nu_t. \]

Where \( X_t = [1, Z_{t-1}, \ldots, Z_{t-p}]' \) and \( \Theta = [d, B_1, \ldots, B_p]' \). By using \( Eu_t'u_t' = H \) and \( \varepsilon_t = A_1^{-1} u_t \), \( \Omega \) is expressed as follows.

\[ \Omega = A_1^{-1} H \left(A_1^{-1}\right)'. \]
In the case of a three-variable VAR model in which parameter Θ and covariance matrix Ω are constant, equation (6) has nine unknown variables, while only six equations are derived from estimates of reduced-form covariance matrix Ω. Therefore, in order to just identify a structural parameter matrix Α, additional restrictions or assumptions are necessary.

The paper first analyzes three-variable VAR models with Clarida and Gali’s (1994) long-run zero restrictions. Next, in order to complement drawbacks of the former method, it estimates the identical VAR models with contemporary sign restriction conditions of Farrant and Peersman (2006). Finally, it compares the estimation results of three-variable VAR models with those of four-variable VAR models in which interest rate variables are additionally considered.


Clarida and Gali (1994) identified structural parameters from reduced-form VAR models with three variables by adding the three long-run restrictions derived from the theoretical model. As shown in table 1, a structural supply shock (υst or νst) has a permanent impact on a relative output level (yt) in the long run. But this is not a case in a structural demand shock (υdt or νdt) and a structural nominal shock (υnt or νnt). Structural supply and demand shocks also influence a long-run level of real exchange rates, whereas

<table>
<thead>
<tr>
<th>Shock Type</th>
<th>y</th>
<th>q</th>
<th>P</th>
</tr>
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<tbody>
<tr>
<td>Supply Shock</td>
<td>( \frac{\partial y_{t,t}}{\partial u_{s,t}} ) ≥ 0</td>
<td>( \frac{\partial q_{t,t}}{\partial u_{s,t}} ) ≥ 0</td>
<td>( \frac{\partial p_{t,t}}{\partial u_{s,t}} ) ≤ 0</td>
</tr>
<tr>
<td>Demand Shock</td>
<td>( \frac{\partial y_{t,t}}{\partial u_{d,t}} ) = 0</td>
<td>( \frac{\partial q_{t,t}}{\partial u_{d,t}} ) ≤ 0</td>
<td>( \frac{\partial p_{t,t}}{\partial u_{d,t}} ) ≥ 0</td>
</tr>
<tr>
<td>Nominal Shock</td>
<td>( \frac{\partial y_{t,t}}{\partial u_{n,t}} ) = 0</td>
<td>( \frac{\partial q_{t,t}}{\partial u_{n,t}} ) = 0</td>
<td>( \frac{\partial p_{t,t}}{\partial u_{n,t}} ) ≥ 0</td>
</tr>
</tbody>
</table>
a structural nominal shock does not have a long-run impact on the real variables such as real output and real exchange rates. But three structural shocks change a relative price level in the long run.

3.2. Farrant and Peersman’s (2006) Contemporary Sign Restrictions

Farrant and Peersman (2006) suggested that a small sample bias and a measurement error could distort the estimation results, when the long-run zero restrictions were imposed. According to the hysteresis theory and some equilibrium growth models, a nominal shock also has a real long-term effect. Therefore, the paper tries to examine the credibility of existing models, by identifying three shocks under the sign restriction assumptions. If the impulse responses of traditional models are similar to the median impulse responses obtained under the sign restriction assumption, the results can be reliable. Table 2 shows the sign restrictions based on Clarida and Gali’s (1994) short-run dynamic model. According to their model, a positive supply shock \( (u_{st}, v_{st}) \) increases relative industrial production \( (y_{t}) \), while decreases relative consumer price \( (p_{t}) \). Real exchange rates \( (q_{t}) \) vary case by case. On the other hand, a positive demand shock \( (u_{dt}, v_{dt}) \) increases relative consumer price as well as relative output, and appreciates real exchange rates. A positive nominal shock \( (u_{nt}, v_{nt}) \) increases relative output and relative consumer prices like a positive demand shock.

| Table 2 | Contemporary Sign Restrictions Based on Clarida and Gali (1994) |
| --- | --- | --- |
| **Supply Shock** | \( \frac{\partial y_{t}}{\partial u_{st}} \geq 0 \) | \( \frac{\partial q_{t}}{\partial u_{st}} \leq 0 \) | \( \frac{\partial p_{t}}{\partial u_{st}} \leq 0 \) |
| **Demand Shock** | \( \frac{\partial y_{t}}{\partial u_{dt}} \geq 0 \) | \( \frac{\partial q_{t}}{\partial u_{dt}} \leq 0 \) | \( \frac{\partial p_{t}}{\partial u_{dt}} \geq 0 \) |
| **Nominal Shock** | \( \frac{\partial y_{t}}{\partial u_{nt}} \geq 0 \) | \( \frac{\partial q_{t}}{\partial u_{nt}} \geq 0 \) | \( \frac{\partial p_{t}}{\partial u_{nt}} \geq 0 \) |
But the former depreciates real exchange rates on the contrary to the latter.

4. ESTIMATION METHODS

This section explains the estimation methods of VAR models with Clarida and Gali’s (1994) long-run restrictions and Farrant and Peersman’s (2006) contemporary sign restrictions. In the impulse response analysis using contemporary sign restrictions, because each of impulse responses is the response based on an individual theoretical model, the effect of a structural shock on the here and the hereafter can be interpreted to be know-nothing. Sign restrictions are also based on a theoretical model such as Clarida and Gali (1994).


Under the assumption of no constant in the three-variable VAR model which satisfies Clarida and Gali’s (1994) long-run zero restrictions, equation (2) can be expressed as the following MA (moving average) form.

\[
Z_t = (A - A_1 L - \cdots - A_p L^p)^{-1} H \nu_t
\]

\[
= \Delta_0 \nu_t + \Delta_1 \nu_{t-1} + \Delta_2 \nu_{t-2} + \cdots
\]

\[
= \Delta(L) \nu_t. \tag{7}
\]

Under the same assumption with equation (7), equation (4) can be represented as the following MA (moving average) form.

\[
Z_t = (I - B_1 L - \cdots - B_p L^p)^{-1} \varepsilon_t
\]

\[
= \varepsilon_t + \Gamma_0 \varepsilon_{t-1} + \Gamma_1 \varepsilon_{t-2} + \cdots
\]

\[
= \Gamma(L) \varepsilon_t. \tag{8}
\]

Equations (7) and (8) show \( \varepsilon_t = \Delta_0 \nu_t = \Delta_0 \mu_t / H^{1/2} \). According to
equations (3) and (4), \( \Delta_0 = A^{-1}H^{1/2} \). Since \( E(\nu', \nu') = I \), \( E(e, e') = \Delta_0 \Delta_0' = \Omega \). In case of the current period \((L=0)\), \( \Delta(0) = \Delta_0 \) and in the long run \((L=1)\), \( \Delta(1) = \Delta_0 + \Delta_1 + \Delta_2 + \cdots \), because \( \Delta(L) = \Delta_0 + \Delta_L + \Delta_2L^2 + \cdots \). Therefore, when the restriction that demand and nominal shocks do not affect long-run output level is assumed like Clarida and Gali (1994), the first row and second column as well as the first row and third column of \( \Delta(1) \) is equal to zero \((\delta_{12}(1) = \delta_{13}(1) = 0)\), respectively. In the same way, when the restriction that a nominal shock does not influence long-run real exchange rates is given, the second row and third column of \( \Delta(1) \) is equal to zero \((\delta_{23}(1) = 0)\).

By using \( \Gamma_0 = I \), \( \Gamma_1 = \Delta_1 \Delta_0^{-1} \), \( \Gamma_2 = \Delta_2 \Delta_0^{-1} \), and so on, which are derived from equations (7) and (8), \( \Gamma(1) = \Gamma_0 + \Gamma_1 + \Gamma_2 + \cdots = \Delta(1) \Delta_0^{-1} \) is obtained. Hence, matrix \( \Gamma(1) \Omega \Gamma(1)' \) is calculated from estimates of \( \Omega \) and \( \Gamma(1) \) gotten from reduced form MA. By utilizing \( E e, e' = \Delta_0 \Delta_0' = \Omega \) and \( \Gamma(1) = \Delta(1) \Delta_0^{-1} \), \( \Gamma(1) \Omega \Gamma(1)' \) can be expressed as follows.

\[
\Gamma(1) \Omega \Gamma(1)' = \Delta(1) \Delta(1)'
\] (9)

When \( M \) is assumed to be the lower triangular matrix obtained from a Cholesky decomposition of \( \Gamma(1) \Omega \Gamma(1)' \), \( MM' \) is represented as follows.

\[
MM' = \Gamma(1) \Omega \Gamma(1)'.
\] (10)

Since a long-run zero restriction implies that \( \Delta(1) \) is lower triangular matrix, \( \Delta(1) \) is equal to \( M \). When \( \Delta(1) = M \) is plugged into \( \Gamma(1) = \Delta(1) \Delta_0^{-1} \), \( \Delta_0 \) is derived as follows.

\[
\Delta_0 = \Gamma(1)^{-1} M.
\] (11)

In short, \( \Delta_0 \) can be identified by using the long-run restriction in which \( \Delta(1) \) is a lower triangular matrix. When the estimates of \( \Delta_0 \) are given, time series of structural shocks and \( \Delta_i \) \((i = 1, 2, \cdots)\) are also identified. The paper dynamically analyzes impacts of structural supply, demand, and
nominal shocks on industrial production, real exchange rates, and prices, respectively, using equation (7) and these estimates.

4.2. Farrant and Peersman’s (2006) Sign Restrictions

In addition to Cholesky decomposition and long-run zero restriction assumptions, structural parameters can be derived by imposing various restrictions based on economic theories on parameters or by using heteroskedasticity of covariance matrix. This section discusses Farrant and Peersman’s (2006) method which identifies an attainable range of impulse response functions by imposing sign restrictions based on economic theories on contemporary structural parameters. Cholesky decomposition and long-run restriction assumptions have the problem that their impulse responses do not necessarily have the signs which are consistent with economic theories. In contrast, from an agnostic point of view, this method focuses on deriving structural shocks to which impulse responses coincide with economic theories from reduced-form shocks. These structural shocks are not also correlated with other shocks and their own lagged shocks.

By making use of relationships between reduced-form and structural shocks discussed above, the estimates of the following structural shocks can be calculated.

\[ \varepsilon_i = \Delta \Delta = \Delta \Delta = \Delta \Delta \]

Where \( A \) is assumed to be a lower triangular matrix on a basis of Cholesky decomposition. \( u_i \) and \( \nu_i \) are the structural shocks of which covariance matrices are \( H \) and \( I \), respectively. By using the square matrix which has a characteristic of \( Q'Q = QQ' = I \), a structural shock \( \nu_i \) can be transformed into a new structural shock \( \nu_i^* \) as follows.

\[ \varepsilon_i = \Delta \nu \]

Where since the covariance matrix of \( \nu_i \) and \( QQ' \) are identity matrices,
the covariance matrix of $\nu_t^*$ are also an identity matrix. Therefore, $\nu_t$ and $\nu_t^*$ have the same covariance matrix, whereas they have different impacts on a reduced-form shock $e_t$ and $Z_t$, as shown in equation (13).

Householder and Givens transformation methods are generally used in order to form an orthogonal matrix $Q$. The study uses the former method. When the Householder transformation method is used in estimation of three-variable VAR models, $3 \times 3$ random variables are extracted from $N(0, I_3)$ and then decomposed using the QR factorization. $\Delta_0^*$ and $\nu_t^*$ are derived by using the orthogonal matrix $Q_H$ obtained from QR decomposition, as shown in equation (13) and then impulse response analyses are carried out. The study gets a lot of impulse response functions through the orthogonal matrix $Q_H$ and considers only the impulse response functions among which contemporary responses satisfy sign restriction conditions.

5. ESTIMATION RESULTS

The paper first estimates three-variable VAR models using real won/dollar exchange rates, Korea and U.S. industrial productions, and consumer prices during the period from January 1990 to May 2015 (Data Source: IMF). Monthly data are considered and the sample size is 305.

5.1. Unit Root and Cointegration Tests

This section first carries out unit root and cointegration tests, before the estimation results are investigated. The unit root test results are represented in table 3, when the lag length is four. Table 3 shows that relative industrial production, relative consumer prices, and real won/dollar exchange rate levels have unit root, while their changes do not have unit root, regardless of the test method or the trend. Table 4 represents the Johansen’s cointegration test results for three variables, when the lag length is four. Three variables do not have a cointegration relation at the 95% level. Therefore, it estimates VAR
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Table 3  Unit Root Test (Lag = 4)

<table>
<thead>
<tr>
<th>Test Method</th>
<th>ADF</th>
<th>PP</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Constant</td>
<td>Trend</td>
</tr>
<tr>
<td>Level</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Industrial Production</td>
<td>–1.264</td>
<td>–1.806</td>
</tr>
<tr>
<td>Consumer Prices</td>
<td>–2.973</td>
<td>–2.121</td>
</tr>
<tr>
<td>Real Won/$ Exchange Rates</td>
<td>–2.467</td>
<td>–2.448</td>
</tr>
<tr>
<td>Difference</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Notes: 1) Industrial production and consumer prices are expressed as a difference between Korea and the US, after taking logarithm for each variable. 2) ** denotes significant in the 1% level.

Table 4  Cointegration Test: Johansen Test (Lag = 4)

<table>
<thead>
<tr>
<th>$H_0$ Variables</th>
<th>$\lambda_{max}$</th>
<th>Criterion (95%)</th>
<th>Trace</th>
<th>Criterion (95%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$r=0$</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Industrial Production, Consumer Prices, Real Won/$ Exchange Rates</td>
<td>X</td>
<td>20.676</td>
<td>21.144</td>
<td>30.566</td>
</tr>
<tr>
<td></td>
<td>O</td>
<td>14.370</td>
<td>24.482</td>
<td>25.208</td>
</tr>
</tbody>
</table>

Notes: 1) Industrial production and consumer prices are expressed as a difference between Korea and the US, after taking logarithm for each variable. 2) $H_0: r=0$ implies the null hypothesis that the cointegration vector does not exist.

models for difference variables.¹)

5.2. Impulse Response Analysis

This section examines two kinds of impulse responses based on Clarida and Gali’s (1994) long-run restrictions and sign restrictions, respectively.²) The lag length is selected to be two, according to AIC, AICc, and SIC criterions. Because the currency crisis and the global financial crisis occurred during the

¹) The estimation results of impulse responses for level variables are also not different from those for difference variables.
²) In cases of Cholesky decomposition, the empirical results are not reported to save space, because they are not reliable.
analysis period, the paper estimates VAR models with the two dummy variables of which each is composed of one for the crisis period, otherwise zero. It considers the period from November 1997 to December 1998 as the currency crisis period. The global financial crisis period is assumed to be the period from September 2008 to June 2009. The Householder and Givens transformations are together used in order to select the contemporary impulse responses which satisfy sign restriction conditions. In case of the Givens transformation method, the study does not find any impulse responses which satisfy all the contemporary sign restriction conditions of Clarida and Gali (1994) shown in table 2. Hence, the empirical analysis make use of the contemporary sign restriction conditions represented in table 5. In table 2, it is assumed that a positive demand shock decreases real exchange rates, while a positive nominal shock increases them. In table 5, however, the impact of demand and nominal shocks on real exchange rates are assumed to be uncertain. It is already well known that interest rates and exchange rates move in the same direction in the Chicago model of exchange rate determination with the flexible price. The contrary is the case in the (New) Keynesian exchange rate model with the sticky price. According to Pavlova and Rigobon (2007), if preference for foreign goods was bigger than that for domestic goods, positive demand shocks increased exchange rates.3)

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3) In Korea, the ratios of final consumption expenditure (private), exports of goods and services, and imports of goods and services to GDP are 49.5%, 49.8%, and 55.1% for the periods from 2010 to 2014, respectively.
The estimation results of impulse responses are represented in figure 1. It displays impulse responses of three variables to each of the three positive shocks. In figure 1, a dashed and dotted line represents median impulse responses obtained from one thousand simulations using three-variable VARs with Clarida and Gali’s (1994) long-run zero restrictions. Solid and dotted lines denote median and 5th and 95th percentile impulse responses obtained from one million simulations using three-variable VARs with sign restrictions, respectively. Zero month implies a contemporary response to a shock. When Clarida and Gali’s (1994) long-run zero restrictions are used, cumulative responses of relative industrial production changes to demand and nominal shocks become zero after 24 months. On the other hand, they have all plus values after 24 months under the sign restriction assumption using the householder transformation method. In case of a positive supply shock, cumulative responses of industrial production changes have plus values without relation to estimation models and forecasting periods.

Figure 1 also shows responses of real won/dollar exchange rate changes to one standard deviation shocks. Under the Clarida and Gali’s (1994) long-run zero restriction assumption, cumulative responses of real won/dollar exchange rate changes to a nominal shock become zero after 24 months. On the other hand, under sign restriction assumptions, their cumulative median response has a minus value after 24 months in contrast with table 2. As already mentioned before, in the Chicago theory of exchange rate determination, interest rates and exchange rates move in the same direction. Under the assumptions of Clarida and Gali’s (1994) long-run zero restrictions, cumulative median responses of real won/dollar exchange rate changes to positive demand shocks have plus values after 24 months, in contrast with table 2. But under the sign restriction assumption, their responses are negative, even though their statistical significance is very low, as fifth and ninety fifth percentiles show. On the other hand, positive supply shocks decrease real won/dollar exchange rates like in Euro area without relation to the models

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4) In the Chicago theory, purchasing power parity always holds. But the Keynesian theory assumes that it holds in the long run.
Figure 1  Impulse Responses (Three-Variable VAR)

Notes: Solid and dotted lines denote median and 5th and 95th percentile impulse responses obtained from one million simulations using three-variable VARs with sign restrictions, respectively. A dashed and dotted line represents median impulse responses obtained from one thousand simulations using three-variable VARs with Clarida and Gali’s (1994) long-run zero restrictions.
used. According to Farrant and Peersman (2006), positive supply shocks depreciate real currency values in England and Japan, whereas appreciate Euro’s value. In case of Canada, responses of real exchange rates do not have a statistical significance.5)

The last column of figure 1 represents cumulative median responses of relative consumer price changes between Korea and the US to one standard deviation shocks. Positive supply shocks decrease consumer prices after 24 months, while the contrary is the case in positive demand and nominal shocks. The results do not depend on the models used. But in case of sign restrictions a fifth percentile has a negative value. It implies that their responses may be uncertain.

5.3. Variance Decomposition Analysis

This section examines variance decomposition of forecasting errors under the assumptions of Clarida and Gali’s (1994) long-run zero restrictions and sign restrictions. The estimation results of variance decompositions are represented in table 6. It shows median variance decompositions obtained from simulations and the numbers in parentheses describe error bands of fifth and ninety fifth percentiles. The top part of table 6 shows variance decompositions of industrial production changes. An explanation ratio of supply shock for variance of industrial production changes exceeds 60%, while that of a nominal shock is less than 3%. The results do not vary largely, depending on the models used.

Table 6 also displays variance decompositions of real won/dollar exchange rate changes. An explanation ratio of a relative demand shock for variance of real exchange rate changes is highest after 24 months without relation to estimation methods. It is higher as an 81.4% in sign restrictions, whereas lower as a 53.2% in Clarida and Gali’s (1994) long-run zero restrictions.

5) The empirical results often show that positive supply shocks lead to an appreciation in other countries. Detken et al. (2002) suggested that this result was caused by real wealth effect and domestic bias of consumption.
Table 6  Variance Decompositions (Three-Variable VAR, 24 Months)

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<thead>
<tr>
<th></th>
<th>Estimation Method</th>
<th>Supply Shock</th>
<th>Demand Shock</th>
<th>Nominal Shock</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Industrial Production</strong></td>
<td>Clarida-Gali</td>
<td>0.786</td>
<td>0.213</td>
<td>0.001</td>
</tr>
<tr>
<td></td>
<td>(0.637, 0.909)</td>
<td>(0.090, 0.360)</td>
<td>(0.000, 0.003)</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Sign Restrictions</td>
<td>0.681</td>
<td>0.284</td>
<td>0.024</td>
</tr>
<tr>
<td></td>
<td>(0.182, 0.899)</td>
<td>(0.065, 0.792)</td>
<td>(0.002, 0.200)</td>
<td></td>
</tr>
<tr>
<td><strong>Real Won/Dollar Exchange Rates</strong></td>
<td>Clarida-Gali</td>
<td>0.463</td>
<td>0.532</td>
<td>0.005</td>
</tr>
<tr>
<td></td>
<td>(0.196, 0.705)</td>
<td>(0.289, 0.797)</td>
<td>(0.001, 0.010)</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Sign Restrictions</td>
<td>0.187</td>
<td>0.814</td>
<td>0.007</td>
</tr>
<tr>
<td></td>
<td>(0.062, 0.722)</td>
<td>(0.249, 0.967)</td>
<td>(0.002, 0.105)</td>
<td></td>
</tr>
<tr>
<td><strong>Consumer Prices</strong></td>
<td>Clarida-Gali</td>
<td>0.121</td>
<td>0.557</td>
<td>0.278</td>
</tr>
<tr>
<td></td>
<td>(0.033, 0.383)</td>
<td>(0.165, 0.789)</td>
<td>(0.135, 0.587)</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Sign Restrictions</td>
<td>0.190</td>
<td>0.815</td>
<td>0.009</td>
</tr>
<tr>
<td></td>
<td>(0.060, 0.801)</td>
<td>(0.238, 0.952)</td>
<td>(0.002, 0.107)</td>
<td></td>
</tr>
</tbody>
</table>

Notes: 1) The numbers in the Table present median variance decompositions obtained from simulations. 2) The numbers in parentheses denote fifth and ninety fifth percentiles, respectively.

According to Farrant and Peersman (2006), under the long-run zero restriction assumption, an explanation ratio of a relative demand shock reaches 84% in England, 75% in Euro area, 80% in Japan, and 89% in Canada, respectively. However, when sign restrictions are utilized instead of long-run zero restrictions, a demand shock’s role becomes weaker, while a nominal shock’s role becomes stronger. On the other hand, this study shows that a demand shock’s role becomes stronger, while a nominal shock’s role does not change remarkably. An explanation ratio of a supply shock is the second highest. In particular, in case of long-run zero restrictions, its ratio arrives at 46.3%. A nominal shock can explain less than 1% of variance of real exchange rate changes, regardless of estimation methods. Farrant and Peersman (2006) found a nominal shock’s important role in explaining exchange rates by using sign restrictions. In spite of using the same method, however, the paper leads to the other conclusion.

The last part of table 6 describes variance decompositions of consumer price changes. Explanation ratios of supply, demand, and nominal shocks for variance of price changes are different from those in the cases of other variables. A demand shock’s explanation ratio for variance of inflation is the highest after 24 months in both cases. But a nominal shock’s explanation...
ratio is the higher in case of Clarida and Gali’s (1994) long-run zero restrictions, while lower in the sign restriction conditions.

5.4. Four-Variable VAR Models

Several studies such as Artis and Ehrmann (2000) and Farrant and Peersman (2006) divided a nominal shock into monetary policy and real exchange rate shocks. This study also analyzes four-variable VAR models which are composed of relative industrial production, relative consumer prices, relative interest rates between Korea and the US, and real won/dollar exchange rates. According to AIC and AICc criteria, two is selected as a lag length. Historically, one part of exchange rate fluctuations may be explained as a response against a monetary shock. When two shocks are considered separately, a real exchange rate shock may be resulted from exchange rate movements which is not explained by time varying premium of exchange rates and fundamentals. But it is likely that real exchange rate shocks may be purely real. Money market rates of IMF are used as interest rates. They are used without taking logarithms and interest rate differential shocks are multiplied by \(-1\) in order to represent positive shocks as expansionary monetary policy shocks. This section investigates only the case of sign restrictions to save space. Table 7 shows contemporary sign restriction conditions for each shock in four-variable VAR models.

Figure 2 displays the estimation results of impulse responses under sign restriction conditions based on the Householder transformation method. It displays impulse responses of four variables to each of the four positive shocks. In figure 2, solid and dotted lines denote median and 5th and 95th percentile impulse responses obtained from ten million simulations using four-variable VAR models with sign restrictions, respectively. A positive supply shock cumulatively increases median industrial production changes, whereas decreases median price and real exchange rate changes. It also drops median interest rate changes in the long run. But the cumulative ninety fifth percentiles in interest rates and real exchange rates have opposite signs against
Table 7  Contemporary Sign Restrictions (Four Variables)

<table>
<thead>
<tr>
<th></th>
<th>( y )</th>
<th>( P )</th>
<th>( r )</th>
<th>( q )</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Supply Shock</strong></td>
<td>( \frac{\partial y_i}{\partial u_s} \geq 0 )</td>
<td>( \frac{\partial p_i}{\partial u_s} \leq 0 )</td>
<td>( \frac{\partial r_i}{\partial u_s} )?</td>
<td>( \frac{\partial q_i}{\partial u_s} )?</td>
</tr>
<tr>
<td><strong>Demand Shock</strong></td>
<td>( \frac{\partial y_i}{\partial u_d} \geq 0 )</td>
<td>( \frac{\partial p_i}{\partial u_d} \geq 0 )</td>
<td>( \frac{\partial r_i}{\partial u_d} \leq 0 )</td>
<td>( \frac{\partial q_i}{\partial u_d} )?</td>
</tr>
<tr>
<td><strong>Monetary Policy Shock</strong></td>
<td>( \frac{\partial y_i}{\partial u_m} \geq 0 )</td>
<td>( \frac{\partial p_i}{\partial u_m} \geq 0 )</td>
<td>( \frac{\partial r_i}{\partial u_m} \leq 0 )</td>
<td>( \frac{\partial q_i}{\partial u_m} )</td>
</tr>
<tr>
<td><strong>Real Exchange Rate Shock</strong></td>
<td>( \frac{\partial y_i}{\partial u_q} \geq 0 )</td>
<td>( \frac{\partial p_i}{\partial u_q} \geq 0 )</td>
<td>( \frac{\partial r_i}{\partial u_q} \leq 0 )</td>
<td>( \frac{\partial q_i}{\partial u_q} \geq 0 )</td>
</tr>
</tbody>
</table>

each cumulative median. It implies that their statistical significance is not strong. A positive demand shock increases median industrial production, price, and interest rate changes, but decreases median real exchange rate changes. A positive monetary policy shock increases median industrial production and price changes, while decreases median interest rate and real exchange rate changes. The relationship between relative Korean interest rates and won/dollar exchange rates does not correspond with a Keynesian theory, but a Chicago theory. A positive real exchange rate shock increases median industrial production, price, and interest rate changes. According to Farrant and Peersman (2006), the influence of a pure real exchange rate shock is strong in the short run, but becomes weaker in the long run. On the other hand, this study suggests that it is strong in the long run as well as the short run for the three variables except industrial production in case of Korea.\(^6\)

Tables 8 shows the estimation results of variance decompositions under sign restrictions. A supply shock is the biggest and a real exchange rate shock is the second biggest in explaining variance of industrial production changes. Explanation ratios of demand and nominal shocks are very low. In case of prices, a real exchange rate shock is the biggest in explaining its variance. In case of interest rates, a real exchange rate shock is the biggest and a supply shock is the second biggest.

\(^6\) The main results do not change for the free floating exchange rate system period from January 1998 to July 2016.
What Are Sources of Real Exchange Rate Fluctuations?

Figure 2  Impulse Responses (Four-Variable VAR, Sign Restrictions)

Note: Solid and dotted lines denote median and 5th and 95th percentile impulse responses obtained from ten million simulations using three-variable VARs with sign restrictions, respectively.
Table 8  Variance Decompositions (Four-Variable VAR, Sign Restrictions, 24 Months)

<table>
<thead>
<tr>
<th>Variables</th>
<th>Supply Shock</th>
<th>Demand Shock</th>
<th>Monetary Policy Shock</th>
<th>Real Exchange Rate Shock</th>
</tr>
</thead>
<tbody>
<tr>
<td>$y$</td>
<td>0.648</td>
<td>0.022</td>
<td>0.013</td>
<td>0.210</td>
</tr>
<tr>
<td></td>
<td>(0.253, 0.864)</td>
<td>(0.003, 0.167)</td>
<td>(0.003, 0.109)</td>
<td>(0.112, 0.629)</td>
</tr>
<tr>
<td>$p$</td>
<td>0.132</td>
<td>0.007</td>
<td>0.034</td>
<td>0.622</td>
</tr>
<tr>
<td></td>
<td>(0.019, 0.722)</td>
<td>(0.003, 0.136)</td>
<td>(0.001, 0.683)</td>
<td>(0.021, 0.959)</td>
</tr>
<tr>
<td>$r$</td>
<td>0.266</td>
<td>0.008</td>
<td>0.096</td>
<td>0.534</td>
</tr>
<tr>
<td></td>
<td>(0.032, 0.709)</td>
<td>(0.001, 0.122)</td>
<td>(0.009, 0.428)</td>
<td>(0.178, 0.882)</td>
</tr>
<tr>
<td>$q$</td>
<td>0.102</td>
<td>0.007</td>
<td>0.038</td>
<td>0.813</td>
</tr>
<tr>
<td></td>
<td>(0.055, 0.562)</td>
<td>(0.003, 0.048)</td>
<td>(0.011, 0.579)</td>
<td>(0.073, 0.936)</td>
</tr>
</tbody>
</table>

Notes: 1) The numbers in the Table present cumulative median impulse responses obtained from simulations. 2) The numbers in parentheses denote fifth and ninety fifth percentiles, respectively.

shock is the second biggest in explaining its variance. In case of real exchange rates, the impacts of real exchange rate and supply shocks on them are also the biggest and the second biggest, respectively. Explanation ratios of demand and monetary policy shocks are low. The paper shows that a role of a monetary policy shock is not important, in contrast with Farrant and Peersman (2006).

5.5. Rolling Regression Analysis

Lastly, the paper carries out rolling regression analyses in order to investigate how the empirical results shown in figures 1 and 2 change through time. Figures 3 and 4 present the empirical results of cumulative impulse responses and variance decompositions based on rolling regressions, respectively. The four-variable VAR models with sign restrictions described in table 7 are adopted as the estimation models. The dummy variables for both crisis periods are also considered in estimation. In rolling regressions, 240 (20-year) samples from 305 samples are chosen in each estimation. Since the first sample among fixed 240 samples is replaced with the new sample in each estimation, total 65 estimation results are presented in figures 3 and 4. The numbers 1 and 65 in $y$ axis in figures show the cumulative
impulse responses for the period from January 1990 to December 2009 and for the period from June 1995 to May 2015, respectively. 7)

As figure 3 shows, in recent years, positive supply shocks decrease won/dollar exchange rates less than before, while positive demand shocks increase rather than decrease them. On the other hand, positive monetary policy shocks bring down won/dollar exchange rates without relation to the time period. As already shown above, the relative fall in domestic interest rates drop exchange rates like in the model of exchange rate determination in which the purchasing power parity is accepted even in the short run. According to domestic empirical results, in Korea in which the stock market is perfectly opened to foreign investors, a fall in domestic interest rates leads to a rise in domestic stock prices, which decrease won/dollar exchange rates through the inflow of foreign capital (e.g., Lee, 2012). When the purchasing power parity assumption is accepted, it is possible for positive supply shocks to decrease won/dollar exchange rates by the fall in relative domestic prices, while the reverse is the case in demand shocks. Pavlova and Rigobon (2007) provided that if preference for foreign goods was bigger than that for domestic goods, positive demand shocks increased exchange rates. Recently, the impacts of supply, demand, monetary policy, and exchange rate shocks on industrial production become weaker. So do the impacts of supply and monetary policy shocks on prices.

Figure 4 describes the empirical results of variance decompositions obtained from the same method as that in figure 3. We can find that the explanation ratios for each variance do not change largely. The explanation ratios of monetary policy shocks for exchange rate volatility seem to be small regardless of the time period, while those of supply shocks increase bigger lately. The explanation ratios of supply shocks for variance of industrial production changes become smaller in recent years. The result is contrary in case of exchange rate shocks. Supply shocks recently explain the larger parts of

7) When 120 (10-year) and 180 (15-year) samples instead of 240 (20-year) samples are even used in rolling regressions, the main results do not largely change. But the shorter the sample period is, the bigger is its volatility as well as small sample bias.
Figure 3 Cumulative Impulse Responses (Four-Variable VAR, Sign Restrictions)

Supply Shock → y
Supply Shock → p
Supply Shock → r
Supply Shock → q

Demand Shock → y
Demand Shock → p
Demand Shock → r
Demand Shock → q

Monetary Policy Shock → y
Monetary Policy Shock → p
Monetary Policy Shock → r
Monetary Policy Shock → q

Exchange Rate Shock → y
Exchange Rate Shock → p
Exchange Rate Shock → r
Exchange Rate Shock → q

Notes: It shows the estimation results of rolling regressions. The first number 1 and the last number 65 in y axis presents cumulative median impulse responses for the period from January 1990 to December 2009 and for the period from June 1995 to May 2015, respectively.
What Are Sources of Real Exchange Rate Fluctuations?

**Figure 4  Variance Decompositions (Four-Variable VAR, Sign Restrictions)**

Supply Shock $\rightarrow y$
Demand Shock $\rightarrow y$
Monetary Policy Shock $\rightarrow y$
Exchange Rate Shock $\rightarrow y$

Supply Shock $\rightarrow p$
Demand Shock $\rightarrow p$
Monetary Policy Shock $\rightarrow p$
Exchange Rate Shock $\rightarrow p$

Supply Shock $\rightarrow r$
Demand Shock $\rightarrow r$
Monetary Policy Shock $\rightarrow r$
Exchange Rate Shock $\rightarrow r$

Supply Shock $\rightarrow q$
Demand Shock $\rightarrow q$
Monetary Policy Shock $\rightarrow q$
Exchange Rate Shock $\rightarrow q$

Notes: It shows the estimation results of rolling regressions. The first number 1 and the last number 65 in y axis presents median variance decompositions for the period from January 1990 to December 2009 and for the period from June 1995 to May 2015, respectively.
inflation variance.

6. POLICY IMPLICATIONS

The empirical results of impulse responses demonstrate that only a supply shock certainly increases industrial production, but that demand and nominal shocks do not. The empirical results of variance decompositions also reveal that explanation ratios of a supply shock for variance of industrial production changes exceed 60% after 24 months without relation to the estimation methods. But a nominal shock’s explanation ratio is less than 3%. Rolling regression analyses also support this conclusion. These empirical results suggest that Korea should carry out the long-term supply policy rather than the short-term demand policy such as monetary and fiscal policies.

Cumulative median responses of real won/dollar exchange rate changes after 24 months to positive nominal and monetary policy shocks have negative values, regardless of the estimation methods. It implies that relative Korean interest rates and won/dollar exchange rates move together in the same direction, as the Chicago theory of exchange rate determination with a flexible price suggests. In case of the US versus several developed countries, interest rates and exchange rates move in the opposite direction, as the (New) Keynesian theory of exchange rate determination theory with a sticky price insists. The domestic studies show the mixed empirical results. They depend on which model is chosen between structural and reduced-form models in case of Korea. It calls on the monetary authority to carefully carry out monetary and foreign exchange policies.

According to the empirical results of variance decompositions, an explanation ratio of a nominal shock for variance of real exchange rate changes is less than 1% after 24 months, regardless of the estimation methods. This conclusion is different from that of Farrant and Peersman (2006) who found the important role of a nominal shock, even though this study uses the same method as them. The won/dollar exchange rate seems to play a role as a
shock absorber.

When put together, the impact of a nominal shock or a monetary policy shock on won/dollar exchange rates is weak. In addition, rolling regression analyses show that the impacts of real and nominal shocks on industrial production become weaker in recent years. These results require the Korean policy authority to cautiously carry out monetary and fiscal policies, and to take direct measures to promote inbound and domestic investments.

7. CONCLUSIONS

The paper examines interrelations between real won/dollar exchange rates and fundamental macroeconomic variables such as relative industrial production, relative prices, and relative interest rates between Korea and the US. It estimates structural VAR models based on the two-country open macroeconomic theory using monthly data from 1990 to date. Clarida and Gali’s (1994) long-run zero restrictions and sign restrictions are used in order to derive structural parameters from reduced-form VAR parameters. The householder transformation method is considered for sign restrictions. The paper investigates what the sources of real exchange rate fluctuations are by comparing the empirical results of impulse responses and variance decompositions.

In three-variable VAR models, a nominal shock does not play an important role in explaining real won/dollar exchange rates in contrast to Farrant and Peersman (2006), even though their sign restrictions as well as Clarida and Gali’s (1994) long-run zero restrictions are used. So, it implies that the won/dollar exchange rate can play a role as a shock absorber. In four-variable VAR models in which a nominal shock is divided into monetary policy and real exchange rate shocks, a monetary policy shock does not play an important role as determinants of real won/dollar exchange rates, while a supply shock has a significant impact on short- and long-term won/dollar exchange rates. Rolling regression analyses also support this conclusion.
They also demonstrate that the impacts of real and nominal shocks on industrial production become weaker lately. These empirical results suggest that Korea as a small open economy should cautiously carry out monetary and fiscal policies and take direct measures to promote inbound and domestic investments.

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